### WRM: Weather Routing Metaheuristic

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Search optimised routes for ships in an environment that changes with the time.

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### Plan

Ship weather routing

WRM : a new approach for ship weather routing

WRM running





Search optimised routes for ships in an environment that changes with the time.

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Plan

- the problem,
- ► WRM approach,
- experimentations.

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Search optimised routes for ships in an environment that changes with the time.

#### **Environmental factors**

- wind (speed, direction),
- waves (direction, height,...),

#### affect ship performances

- consumption,
- progression,



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SOG with 15-knots wind, power levels 5 kW, 10 kW, 15 kW, 25 kW, 50 kW

### Ship weather routing : Route



#### Route :

- a trajectory,
- ▶ a value representing the *speed* at each point of the trajectory.

#### speed parameter

► SOG, engine power level, shaft rotation speed,...



Optimize :

- cost,
- safety, green gazes emissions, comfort, duration,...

 $\label{eq:constraints} \textbf{Constraints}: \mathsf{dates}, \, \mathsf{forbidden/penalized} \, \mathsf{regions}, \, \mathsf{bad} \, \mathsf{weather} \\ \mathsf{conditions}, \ldots$ 

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The search space is continuous in space as in time

#### **Publications** :



Fig. 2. Publishing trend in the area of ship weather routing and voyage optimization. Source: Scopus February 2020.

Zis, T.P., Psaraftis, H.N., Ding, L. : Ship weather routing : A taxonomy and survey. Ocean Engineering 213, 107697 (2020).

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Existing approaches :

isochrones, isopones : time/fuel consumption,

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- dynamic programming : 2D, 3D,
- Dijkstra based algorithms,
- genetic algorithms,

Existing approaches :

- isochrones, isopones : time/fuel consumption,
- dynamic programming : 2D, 3D,
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- genetic algorithms,

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#### WRM : metaheuristic

Iaunch many times a simple forward algorithm on simplified versions of the problem

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Grandcolas, S., A metaheuristic algorithm for ship weather routing, to appear in *Operations Research Forum*, 2022. DOI : 10.1007/s43069-022-00140-0

### Existing approaches



"Multi-Objective Optimization of Motor Vessel Route." Marie, S., Courteille, E. 2009



"Development of a novel forward dynamic programming method for weather routing" Shao, W., Zhou, P., Thong, S. 2011



### Existing approaches



"An Ant Colony Algorithm for efficient ship routing." Tsou, M.C., Cheng, H.C. 2013



"The optimization of ship weather-routing algorithm based on the composite influence of multi-dynamic elements." Fang, M.C., Lin, Y.H. 2015



"Minimizing the fuel consumption and the risk in maritime transportation : A bi-objective weather routing approach" Veneti, A., Makrygiorgos, A., Konstantopoulos, C., Pantziou, G., Vetsikas, I. 2017





"Multi-Objective Weather Routing of Sailing Vessels." Życzkowski, Marcin and Rafal Szlapczynski. 2017

### Existing approaches : 3D dynamic programming



Kim, K.I., Lee, K.M. : Dynamic Programming-Based Vessel Speed Adjustment for Energy Saving and Emission Reduction. Energies 11(5) (2018).

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### Existing approaches : Dijkstra's algorithm





Fig. 3. An illustration of the 3D graph (a grid of waypoints) system for voyage optimization.

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Wang, H., Mao, W., Eriksson, L. : A Three-Dimensional Dijkstra's algorithm for multi- objective ship voyage optimization. Ocean Engineering 186, 106131 (2019).

### WRM : Weather Routing Metaheuristic

Ship weather routing

WRM : a new approach for ship weather routing

WRM running



### WRM

#### Problem :

- departure, destination,
- a time window,
- a weather forecast,
- speed parameter : engine power level

#### Goal : find a route whose total cost is minimal

The idea : solve a series of simplified versions of the problem gradually focusing on the most promising area.



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$$P = \{p_0, p_1, \dots, p_n\} \\ L = \{(p_i, p_j), p_i, p_j \in P\} \\ W = \{l_1, l_2, \dots, l_m\} \\ [t_{min}, t_{max}] \\ \mathcal{F}$$

points legs power level values time window weather forecast

(P, L): directed, acyclic.



$$P = \{p_0, p_1, \dots, p_n\} \\ L = \{(p_i, p_j), p_i, p_j \in P\} \\ W = \{l_1, l_2, \dots, l_m\} \\ [t_{min}, t_{max}] \\ \mathcal{F}$$

points legs power levels time window weather forecast

**Route :** 
$$(t_{dep}, (u_0, u_1, ..., u_k), (w_0, w_1, ..., w_{k-1}))$$

for each *i*,  $(u_i, u_{i+1}) \in L$  and  $w_i \in W$ , constant power level on each leg.

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### Evaluation of crossings :

- ► duration(u, v, w, t, F)
- $cost(u, v, w, t, \mathcal{F})$



duration and cost to cross from u to v at the date t at engine power level w, given the forecast  $\mathcal{F}$ .

#### Evaluation of crossings :

- ▶ duration(u, v, w, t, F)
- $cost(u, v, w, t, \mathcal{F})$



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$$\textit{P} = \textit{P}_{\textit{idle}} + (\textit{P}_{\textit{calm}} + \textit{P}_{\textit{wind}}) imes \textit{C}_{\textit{waves}}$$

#### Evaluation of crossings :

- ► duration(u, v, w, t, F)
- $cost(u, v, w, t, \mathcal{F})$



$$P = P_{idle} + (P_{calm} + P_{wind}) imes C_{waves}$$

$$\begin{aligned} P_{calm} &= c_1 \times v^{2.5} \\ P_{wind} &= c_2 \times A \times s_a^2 \times \cos \theta_a \\ C_{waves} &= f(\lambda, L, \theta_w, v) \end{aligned}$$

- v:SOG
- A : projected surface area
- $\theta_{a}$  : apparent wind to ship angle
- sa : apparent wind speed
- $\lambda$  : waves length
- L : ship length
- $\theta_w$  : waves to ship angle



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Valid route : 
$$\langle t_{dep}, (u_0, u_1, \ldots, u_k), (w_0, w_1, \ldots, w_{k-1}) \rangle$$

satisfies

$$t_{dep} \geq t_{min}$$
 and  $t_{arr} \leq t_{max}$ 

where  $t_{arr}$  is the arrival date

### WRM : searching a good route

**Dated costs :** (u, t, c)

there is a route that reaches u at date t whose cost is c



**Combinatorial explosion** : discard the dated costs that seem the least promising.

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Best route : Arrival best dated cost.

#### Improvements :

- minimal arrival dates (forward exploration),
- maximal arrival dates (backward exploration),
- minimal bounds of the costs,

#### Number of legs evaluations :

```
\mathcal{O}(|L|\times |W|\times K)
```

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K : given limit of the number of dated costs for each vertex

### WRM : Metaheuristic algorithm

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algorithm WRM (dep, dest, t_{min}, t_{max}, P_{min}, P_{max}, \mathcal{F}, nb_{runs})

\pi := initial parameters,

repeat nb_{runs} times

\pi-generate a simplified problem \mathcal{P},

solve \mathcal{P} propagating dated costs,

update bestRoute,

update \pi,

end loop

return bestRoute,
```

- first runs : unconstrained generation,
- following runs : strengthen  $\pi$  parameters step by step, so as to converge towards the most promising areas

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#### Generate problem



#### Search a good route



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#### Mark surrounding area



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#### Generate problem



#### Search a route



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#### Mark surrounding area



#### Strengthen generation parameters



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- perimeter,
- time windows,
- steps and ranges of the power levels.

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### WRM : Marseille-Chypre [130h, 260h]



### $l{=}1581.5NM/1394.1NM$ sp=12.2kn cost=2101399.2 130.0h-260.0h (130.0h) (16 mar 10h00 to 21 mar 19h57) 57 points 141.6s

Forecast : NOAA (National Oceanic and Atmospheric Administration), GFS atmospheric and waves models, 384h, 3 hours intervals, resolution  $0.25^\circ.$ 

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### WRM : Marseille-Chypre [130h, 260h], shortest route





#### Direct route (simulation) :

- 1451.2 nautic miles,
- 128.5 hours,
- cost 4315241 (constant power 31.5kw)

#### Route returned by WRM :

- 1581.5 nautic miles,
- 130.0 hours (avg speed 12.2 knots),

cost 2101399

cost at idle : 677237

### WRM : Marseille-Chypre penalize bad weather conditions

Training of the second se			
	w	ind speed ind heading	$\ge$ 22 knots $\le$ 120 $^{\circ}$
36 mar 10h00 +130h	w. w	aves height aves heading	$\ge$ 1.5 m $\ge$ 10 $^{\circ}$

### $l{=}1703.9NM/1394.1NM$ sp=16.3kn cost=3704002.4 155.5h-260.0h (104.5h) (17 mar 11h27 to 21 mar 19h59) 50 points 309.8s

 $l{=}1581.5NM/1394.1NM$  sp=12.2kn cost=2101399.2 130.0h-260.0h (130.0h) (16 mar 10h00 to 21 mar 19h57) 57 points 141.6s

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### WRM : Marseille-Chypre ECA [130h, 260h]



#### ECA (Emission Control Areas) : cost increase 20%

### $l{=}1631.4NM/1394.1NM$ sp=12.8kn cost=2191371.0 132.5h-260.0h (127.5h) (16 mar 12h27 to 21 mar 19h59) 57 points 103.2s

 $l{=}1581.5NM/1394.1NM$  sp=12.2kn cost=2101399.2 130.0h-260.0h (130.0h) (16 mar 10h00 to 21 mar 19h57) 57 points 141.6s

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### WRM : Marseille-Chypre ECA [130h, 260h]



 $l{=}1737.9NM/1394.1NM$  sp=13.4kn cost=2501611.2 130.0h-260.0h (130.0h) (16 mar 10h00 to 21 mar 20h01) 59 points 54.4s

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